

Bab 6. Elemen Pengindera (Sensing Element)

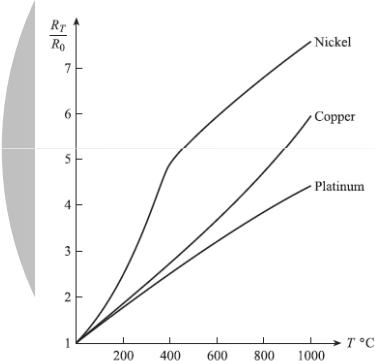
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Resistive metal and semiconductor sensors for temperature measurement

$$R_T = R_0(1 + \alpha T + \beta T^2 + \gamma T^3 + \dots)$$



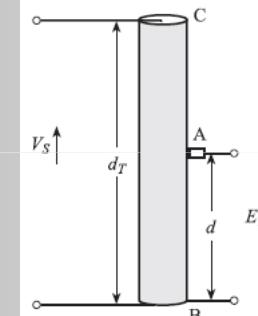
Platinum

- ❖ $R_0 = 100.0 \Omega$, $R_{100} = 138.50 \Omega$, $R_{200} = 175.83 \Omega$,
- ❖ $\alpha = 3.91 \times 10^{-3} \text{ }^\circ\text{C}^{-1}$ and $\beta = -5.85 \times 10^{-7} \text{ }^\circ\text{C}^{-2}$.

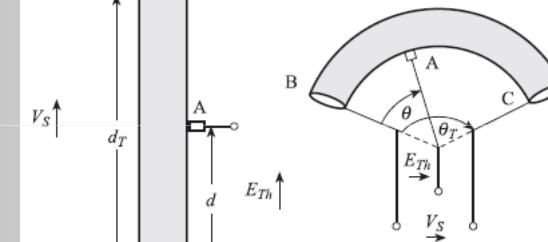
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Resistive sensing elements

Potentiometer Displacement Sensor



(a) Linear (rectilinear)
displacement



(b) Angular (rotary)
displacement

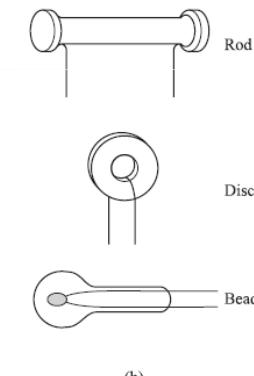
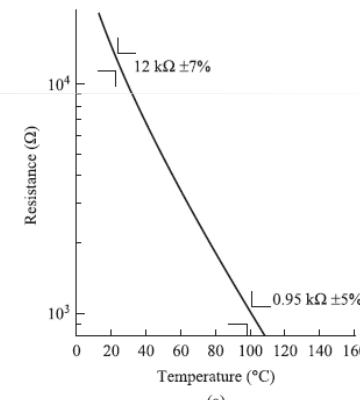
$$E_{Th} = V_S x = V_S d / d_T$$

$$E_{Th} = V_S \theta / \theta_T = V_S x$$

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Termistor

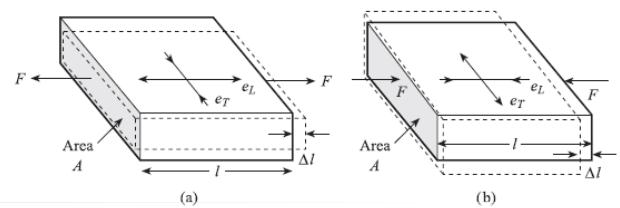
$$R_\theta = R_{\theta_1} \exp \beta \left[\frac{1}{\theta} - \frac{1}{\theta_1} \right]$$



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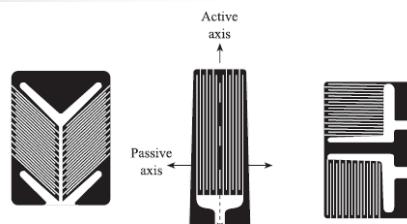


Metal and semiconductor resistive strain gauges (Piezoelectric Effect)



Stress and strain:
 (a) Effect of tensile stress
 (b) Effect of compressive stress.

Gauge factor 2.0 to 2.2
 Unstrained resistance $120 \pm 1 \Omega$
 Linearity within $\pm 0.3\%$
 Maximum tensile strain $+2 \times 10^{-2}$
 Maximum compressive strain -1×10^{-2}
 Maximum operating temperature 150°C .

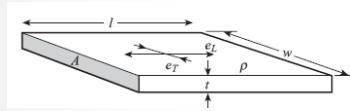


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Perhitungan Straingauge

$$\Delta R = \left(\frac{\partial R}{\partial l} \right) \Delta l + \left(\frac{\partial R}{\partial A} \right) \Delta A + \left(\frac{\partial R}{\partial \rho} \right) \Delta \rho$$



Gauge Factor :

$$G = 1 + 2\nu + \frac{1}{e} \frac{\Delta \rho}{\rho}$$

V=poisson ratio (0,25-0,44)
 e = elastisitas
 ρ = tahanan dalam

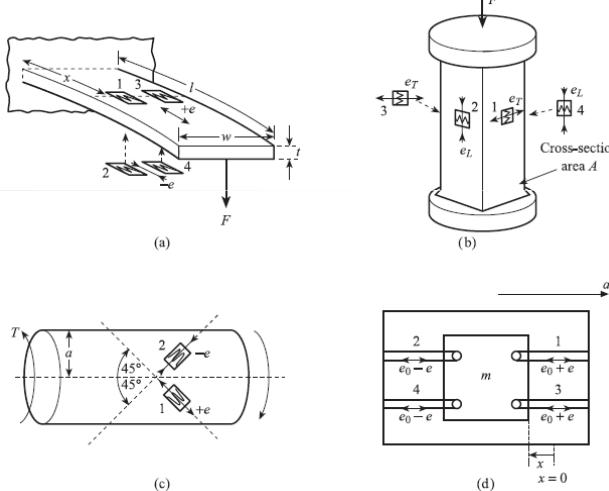
$$\frac{\Delta R}{R_0} = Ge$$

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Practical elastic sensing elements using strain gauges

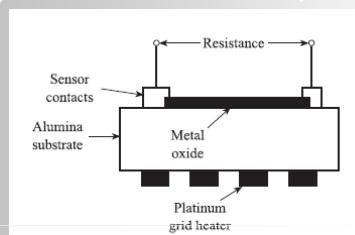
Figure 8.20 Practical elastic sensing elements using strain gauges:
 (a) Cantilever load cell
 (b) Pillar load cell
 (c) Torque sensor
 (d) Unbonded strain gauge accelerometer.



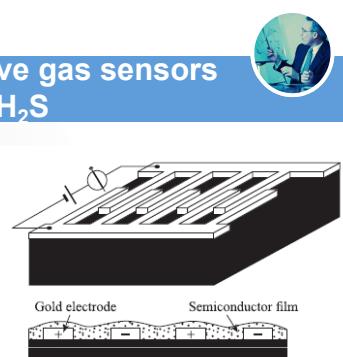
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Semiconductor resistive gas sensors (HCl, NO₂, H₂S)

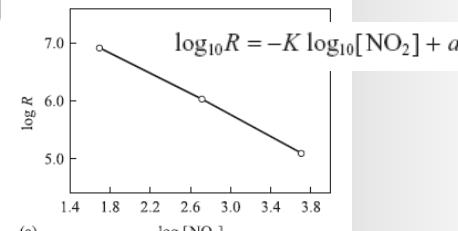


(b)



(c)

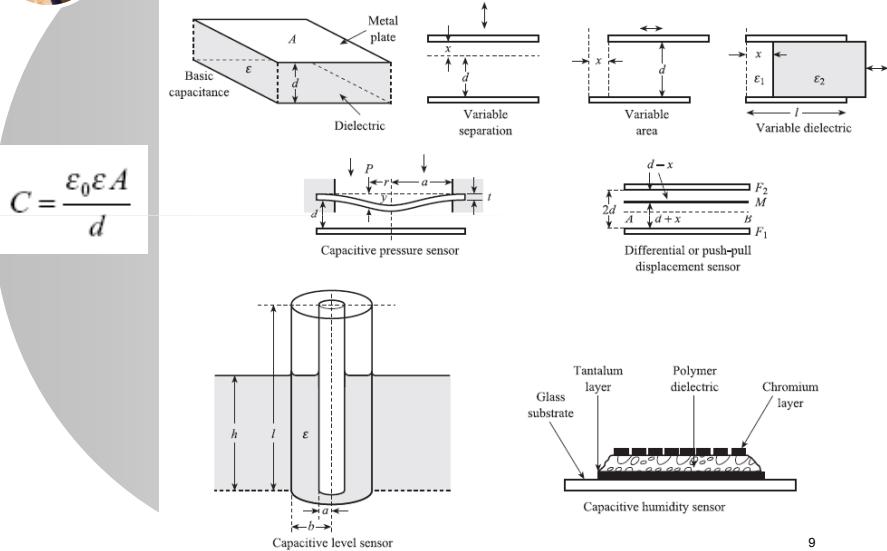
Untuk NO₂



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Capacitive sensing elements



Capacitive sensing elements

$$C = \frac{\epsilon_0 \epsilon A}{d + x}$$

Variable separation displacement sensor

$$C = \frac{\epsilon_0 \epsilon A}{d}$$

Capacitive Humidity sensor

$$\frac{\Delta C}{C} = \frac{(1 - v^2)a^4}{16Edt^3} P$$

Capacitive pressure sensor

$$C_h = \frac{2\pi\epsilon_0}{\log_e\left(\frac{b}{a}\right)} [l + (\epsilon - 1)h]$$

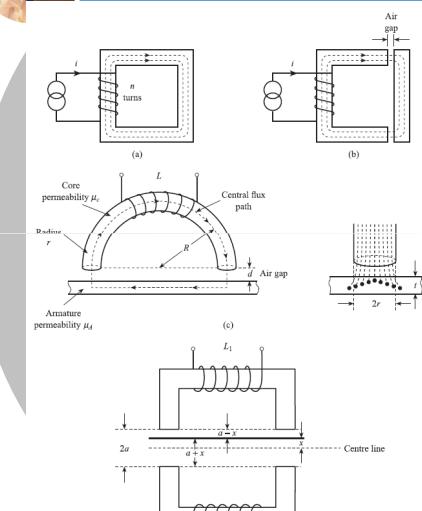
Capacitive level sensor

Source: John P. Bentley
Principles of Measurement System

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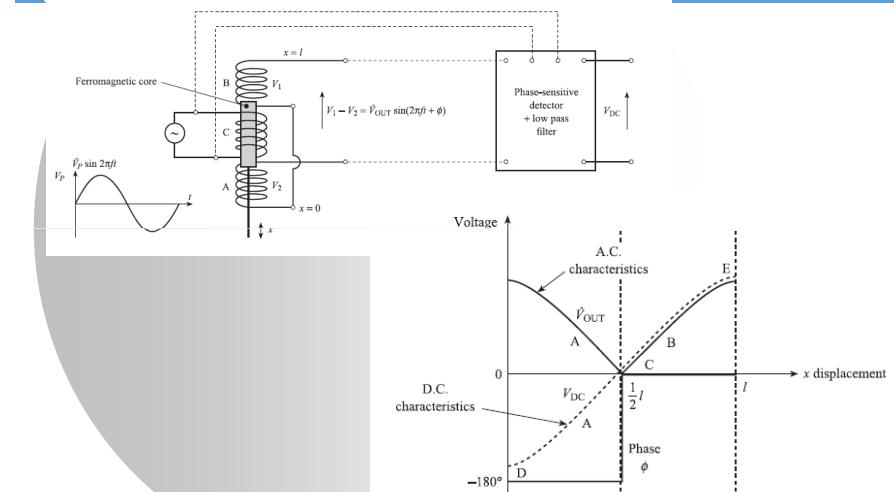
Inductive sensing elements



L = Induktansi
N = Total Fluks
i = Arus
n = jumlah lilitan
R = Reluktansi

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Linear Variable Differential Transformer (LVDT) displacement sensor





Electromagnetic sensing elements

$$E = -\frac{dN}{dt}$$

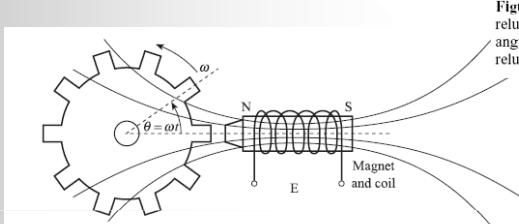
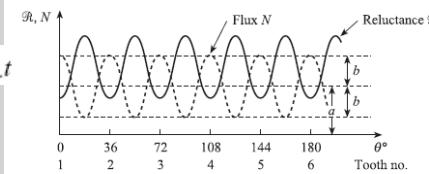


Figure 8.15 Variable reluctance tachogenerator, angular variations in reluctance and flux.

$$E = bm\omega_r \sin m\omega_r t$$

m = nomor gigi



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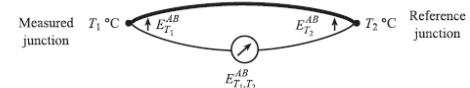


Thermoelectric sensing elements

Figure 8.16 Thermocouple principles.

$$E_{T_1,T_2}^{AB} = E_{T_1}^{AB} - E_{T_2}^{AB} \\ = a_1(T_1 - T_2) + a_2(T_1^2 - T_2^2) + a_3(T_1^3 - T_2^3) + \dots$$

Thermocouple circuit

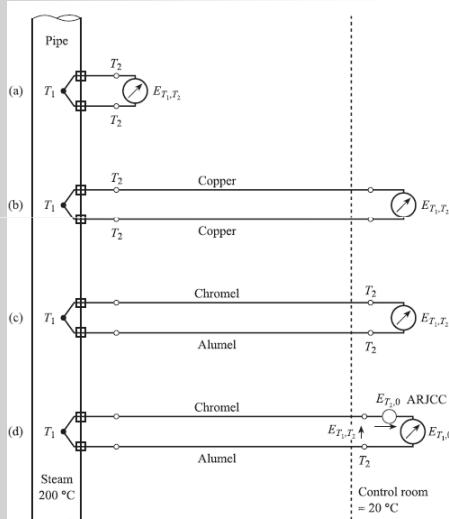


Thermocouple laws

$$\begin{aligned} \text{Law 1} \quad & T_1 \xrightarrow{\text{A}} T_3 \xrightarrow{\text{B}} T_5 \xrightarrow{\text{A}} T_4 \xrightarrow{\text{B}} T_6 \xrightarrow{\text{A}} T_2 \equiv T_1 \xrightarrow{\text{A}} T_7 \xrightarrow{\text{B}} T_9 \xrightarrow{\text{A}} T_8 \xrightarrow{\text{B}} T_{10} \xrightarrow{\text{A}} T_2 \\ \text{Law 2} \quad & T_1 \xrightarrow{\text{A}} T_2 \equiv T_1 \xrightarrow{\text{A}} T_3 \xrightarrow{\text{B}} T_7 \xrightarrow{\text{A}} T_8 \xrightarrow{\text{B}} T_2 \\ \text{Law 3} \quad & T_1 \xrightarrow{\text{A}} T_2 \equiv T_1 \xrightarrow{\text{A}} T_2 \xrightarrow{\text{B}} T_3 \xrightarrow{\text{A}} T_2 \\ \text{Law 4} \quad & T_1 \xrightarrow{\text{A}} T_2 \equiv T_1 \xrightarrow{\text{A}} T_2 \xrightarrow{\text{B}} T_3 \xrightarrow{\text{C}} T_2 + T_1 \xrightarrow{\text{A}} T_2 \xrightarrow{\text{B}} T_3 \xrightarrow{\text{C}} T_2 \\ \text{Law 5} \quad & T_1 \xrightarrow{\text{A}} T_2 \equiv T_1 \xrightarrow{\text{A}} T_2 \xrightarrow{\text{B}} T_3 \xrightarrow{\text{A}} T_2 + T_3 \xrightarrow{\text{A}} T_2 \xrightarrow{\text{B}} T_2 \end{aligned}$$



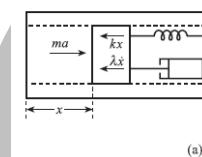
Termocouple Instalation



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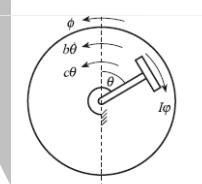
Elastic sensing elements



(a)

$$\begin{aligned} m\ddot{x} + \lambda\dot{x} + kx &= ma \\ \frac{\Delta\ddot{x}}{\Delta a}(s) &= \frac{1}{\omega_n^2} s^2 + \frac{2\xi}{\omega_n} s + 1 \\ \omega_n &= \sqrt{\frac{k}{m}}, \xi = \frac{\lambda}{2\sqrt{km}}, K = \frac{1}{\omega_n^2} \end{aligned}$$

$$\begin{aligned} m\ddot{x} + \lambda\dot{x} + kx &= AP \\ \frac{\Delta\ddot{x}}{\Delta P}(s) &= \frac{1}{\omega_n^2} s^2 + \frac{2\xi}{\omega_n} s + 1 \\ \omega_n &= \sqrt{\frac{k}{m}}, \xi = \frac{\lambda}{2\sqrt{km}}, K = \frac{A}{k} \end{aligned}$$



(c)

$$\begin{aligned} I\ddot{\theta} + b\dot{\theta} + c\theta &= I\phi \\ \frac{\Delta\ddot{\theta}}{\Delta I}(s) &= \frac{1}{\omega_n^2} s^2 + \frac{2\xi}{\omega_n} s + 1 \\ \omega_n &= \sqrt{\frac{c}{I}}, \xi = \frac{b}{2\sqrt{cI}}, K = \frac{1}{\omega_n^2} \end{aligned}$$

$$\begin{aligned} I\ddot{\theta} + b\dot{\theta} + c\theta &= T \\ \frac{\Delta\ddot{\theta}}{\Delta T}(s) &= \frac{1}{\omega_n^2} s^2 + \frac{2\xi}{\omega_n} s + 1 \\ \omega_n &= \sqrt{\frac{c}{I}}, \xi = \frac{b}{2\sqrt{cI}}, K = \frac{I}{c} \end{aligned}$$

Figure 8.19 Dynamic models of elastic elements:
(a) Linear accelerometer
(b) Pressure sensor
(c) Angular accelerometer
(d) Torque sensor.



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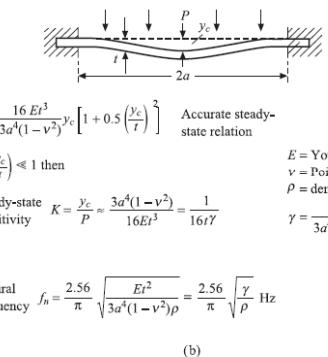
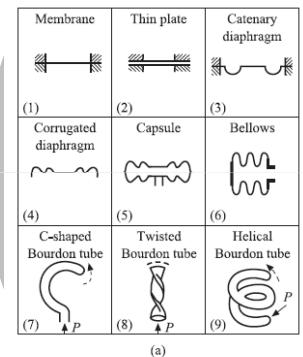


Figure 8.21 Elastic pressure sensing elements:
(a) Different types (after Neuber^[12])
(b) Flat circular diaphragm.

$$P = \frac{16 E t^3}{3a^4(1-\nu^2)} \gamma_c \left[1 + 0.5 \left(\frac{\gamma_c}{t} \right)^2 \right]$$

Accurate steady-state relation

E = Young's modulus

ν = Poisson's ratio

ρ = density

$$\text{Steady-state sensitivity } K = \frac{\gamma_c}{P} \approx \frac{3a^4(1-\nu^2)}{16Et^3} = \frac{1}{16t\gamma}$$

$$\gamma = \frac{Et^2}{3a^4(1-\nu^2)}$$

and

$$\text{Natural frequency } f_n = \frac{2.56}{\pi} \sqrt{\frac{Et^2}{3a^4(1-\nu^2)\rho}} = \frac{2.56}{\pi} \sqrt{\frac{\gamma}{\rho}} \text{ Hz}$$

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Ion selective electrodes



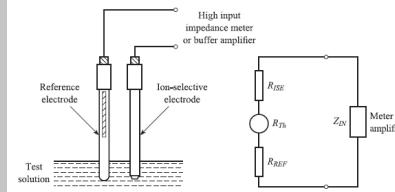
Figure 8.25

Ion-selective electrodes:
(a) Basic system for ion concentration measure and equivalent circuit

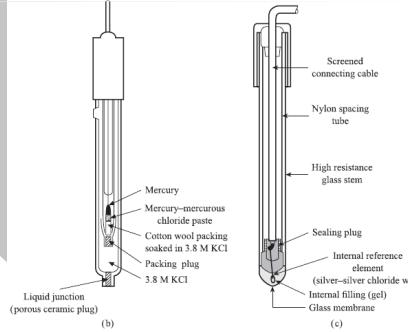
(b) Calomel reference electrode (after Bailey^[17]), © P. L. Bailey 1980.

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(c) Practical pH sensor (after Thompson^[18]).



(a)



(b)



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